Nanoscale temperature mapping in operating microelectronic devices

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Modern microelectronic devices have nanoscale features that dissipate power nonuniformly, but fundamental physical limits frustrate efforts to detect the resulting temperature gradients. Contact thermometers disturb the temperature of a small system, while radiation thermometers struggle to beat the diffraction limit. Exploiting the same physics as Fahrenheit’s glass-bulb thermometer, we mapped the thermal expansion of Joule-heated, 80-nanometer-thick aluminum wires by precisely measuring changes in density. With a scanning transmission electron microscope and electron energy loss spectroscopy, we quantified the local density via the energy of aluminum’s bulk plasmon. Rescaling density to temperature yields maps with a statistical precision of 3 kelvin/hertz, an accuracy of 10%, and nanometer-scale resolution. Many common metals and semiconductors have sufficiently sharp plasmon resonances to serve as their own thermometers.

High-resolution thermometry is under constant development in many arenas. Some approaches involve inserting local probes [even miniature expansion thermometers (12)] that can be queried remotely. For instance, luminescent nanoparticles inserted in biological systems can measure intracellular temperature gradients (9), or low-melting point metals deposited on a solid-state device can provide a binary temperature determination (13, 14). Alternatively, the thermometer can be external and mobile. Scanning probe techniques include scanning thermal microscopy (SThM), in which the tip of an atomic force microscope is equipped with a thermocouple or resistive sensor (15, 16), and near-field scanning optical microscopy, in which a fiber is used to beat the far-field diffraction limit (4, 5, 11, 17). Both of these methods can achieve resolution ≤50 nm (16, 17). Perhaps most like the work described here, nuclear magnetic resonance (NMR) (18), electron backscatter diffraction (19), or inelastic electron scattering (20) can induce the measured system to provide its own thermometric signal. Of these three, only the NMR technique has demonstrated mapping with millimeter-scale resolution (18). Of all of the aforementioned methods, none have demonstrated detailed temperature maps with sub-10-nm spatial resolution.

Here, we describe a noncontact, thermometric technique that can measure bulk temperatures with nanometer-scale spatial resolution: plasmon energy expansion thermometry (PEET). Based on electron energy loss spectroscopy (EELS), the technique is noncontact in the sense that the measurement has a negligible effect on the measured system’s temperature. Like Fahrenheit’s mercury-in-glass thermometer, this thermometer derives its sensitivity and accuracy from the calibrated thermal expansion of a conventional material—here, aluminum. As outlined in Fig. 1A, we applied EELS in a scanning transmission electron microscope (STEM) to measure the energy required to excite a bulk plasmon in the metal. In the free-electron model, this energy is given by

\[
E = \hbar \omega_p = \hbar \sqrt{\frac{4\pi ne^2}{m}}
\]

where \(\hbar\) is the reduced Planck constant, \(\omega_p\) is the plasmon angular frequency, and \(n\) is the number density of valence electrons with charge \(e\) and mass \(m\). At room temperature \((T_0)\), aluminum has \(n(T_0) = 1.8 \times 10^{29} \text{ m}^{-3}\), which gives \(E(T_0) = 15.8 \text{ eV}\) according to Eq. 1. This value is within 3% of the measured value of 15.2 eV (21), demonstrating the applicability of the free electron model in aluminum.

The plasmon energy is temperature-sensitive because thermal expansion changes the number density according to \(n(T) = n(T_0)\left[1 - \frac{T}{T_0}\right]\), where \(\alpha(T) = \frac{T}{T_0} n(T_0) \frac{\partial n(T_0)}{\partial T} + \omega_p^2\) and \(\alpha\) is the coefficient of linear thermal expansion (21-23). The normalized change in the plasmon energy \(R = (E(T) - E(T_0))/E(T_0)\) is thus related to the temperature change \(\Delta T\) by a quadratic equation with solution

\[
\Delta T = T - T_0 = \frac{c_1}{2a_2} \left( \sqrt{1 - \frac{8R a_2}{3a_1^2}} - 1 \right)
\]

In aluminum, the coefficients \(c_1 = 23.5 \times 10^{-6} \text{ K}^{-1}\) and \(a_2 = 8.9 \times 10^{-9} \text{ K}^{-2}\) approximate \(\alpha(T)\) to better than 2% over the range from 25 to 650°C (24, 25). By focusing the STEM electron beam into a nanometer-sized probe, rastering it over the sample, and analyzing the shift of the plasmon peak in the EELS spectrum according to Eq. 2, we produced a temperature map.

With a plasmon peak width ~1.3 eV, the peak shift of roughly ~0.54 meV/K (in the linear approximation) is too subtle to reliably detect by merely locating the peak maximum. However, curve-fitting improves our sensitivity to energy or temperature shifts by almost an order of magnitude (26). The shift for a large (120 K) temperature difference is shown in Fig. 1B, measured with a spectrum integration time of 26 ms. Under such imaging conditions, repeated measurements at a single point give standard deviations in the energy loss of 8 to 12 meV, which is equivalent to 15 to 21 K. For spectrum acquisition rates of 30 to 76 s, the plasmon energy sensitivity scales like shot noise with slope ~1.7 meV/s, which is equivalent to 3 K/\(\sqrt{\text{Hz}}\).

To demonstrate PEET’s spatial resolution, we used electron-beam lithography to fabricate a variety of serpentine aluminum devices that exhibit temperature gradients on submicrometer-length scales (Fig. 1C). Depending on the contacts used, a device can be Joule-heated locally by applying a voltage across it, or remotely by heating its neighbor (26).

Local heating gives PEET maps such as Fig. 1D. The map contains 336 by 223 pixels with an 11-nm pitch and is derived from two EELS spectrum images, one acquired at room temperature and
the other at elevated temperature. Thus, each pixel has two associated spectra similar to those shown in Fig. 1B. Averaging over 64 pixels in the indicated square regions gives standard errors of 2 and 3 K respectively, showing a temperature difference $\pm 4$ K with a signal-to-noise ratio of 20. The highest temperatures are not found at the wire’s midpoint, as would be expected for a straight and uniform one-dimensional conductor, but rather in the sections farthest from the lead connections. PEET reveals that the midpoint loses heat to the cooler end legs (only 150 nm away) through the Si$_3$N$_4$ membrane and via near-field electromagnetic transport (II).

The PEET analysis procedure is described in more detail in Fig. 2, which shows raw maps of the plasmon energy for a device with zero (Fig. 2A) and nonzero (Fig. 2B) power applied to a remote heater. In both cases, the sensitive curve-fitting procedure reveals nanometer-scale structures in the aluminum. Most noticeable in the leads, these structures are due to grain boundaries, which show a plasmon energy decrease of $\Delta E = 13 \pm 12$ meV (figs. S1 and S2). The implied density decrease of $\Delta n/n \approx 2 \Delta E/E \approx 0.2\%$ is expected because of the grain boundary volume excess (27). Without correction, the grain boundary shift would give a false temperature offset of ~24 K. The subtraction in the normalized plasmon shift ratio $R = (B - A)/A$ (where the letters refer to the respective panels of Fig. 2) suppresses this potential systematic, leaving residuals that are barely evident in the temperature map in Fig. 2C (fig. S3).

The map in Fig. 2C shows a steady warming with distance from the lower contact, a trend

**Fig. 1. Experiment overview.** (A) Apparatus: a STEM, a biasing sample holder, a power source for Joule-heating the sample, and an EELS spectrometer. (B) Aluminum EELS data characteristic of 293 K (black) and 413 K (red). The vertical lines in the inset indicate the plasmon peak centers, as determined by curve-fitting, and the arrows indicate the peak maxima. (C) Scanning electron microscope image of an example device architecture. Four leads connect to three Al device geometries over an electron-transparent, Si$_3$N$_4$ membrane. (D) A false-color temperature map of a 80-nm-thick, 100-nm-wide serpentine aluminum wire Joule-heated by the application of 161 $\mu$A. The histogram indicates the color scale and bins each pixel according to its temperature. The average temperatures measured in the indicated 86- by 86-nm squares are 310 $\pm$ 2 K (bottom left) and 390 $\pm$ 3 K (top right).

**Fig. 2. Remote heating.** (A and B) Plasmon energy map with 4-nm pixels of a 100-nm-thick aluminum wire (A) at room temperature and (B) with 2 mW applied to a heater outside the field of view. (C) Temperature map constructed from (A) and (B). White bars indicate the 90- by 10-pixel segments used to generate the (D) line profiles and (E) histograms. Narrow lines and histograms show data averaged over 40 nm vertically, and dots connected by thicker lines indicate data averaged over 40 nm in both directions.
In situ thermal studies with nanoscale thermometry can use temperature control elements that are smaller and thus faster. This advantage enables rapid heating and quenching experiments and better control of systematics. For instance, annealing at elevated temperatures causes grain boundaries to reconfigure. But with a small heater over the electron-transparent window, the temperature can be cycled without pausing to wait for thermal drift to stabilize. Thus, the $T_0$ reference map can be frequently refreshed, mitigating this systematic without incurring a large duty-cycle penalty.

Shown in Fig. 3 is how the temperature of an aluminum contact, here heated remotely, can be changed by hundreds of kelvins in real time, without disturbing the temperature measurement or causing the burdensome thermal drift typical of furnace-style heating sample holders. These data depict an EELS spectrum image acquisition in which the power to the remote heater was ramped down in steps, with zero-power intervals separating each new nonzero value from the previous one (Fig. 3A). Heating effects are nearly undetectable in the annular dark field (ADF) images corresponding to zero power (Fig. 3C) and stepped power (Fig. 3D). Grain rotation induced some tiny contrast changes, and the drift was sufficiently small to be handled by the EELS data acquisition software’s automated drift correction routine, which executed every two rows.

Comparison of the ADF and plasmon energy images also emphasizes the common origin of the structure evident in the zero-power ($T_0$) images—grains. The ADF image shows diffraction contrast varying randomly from grain to grain based on the local lattice orientation, whereas the plasmon energy image highlights the grain boundaries because of the volume excess effect discussed above (figs. S1 and S2). In the temperature map (Fig. 3G), a few grain boundaries show residuals 3 to 4 standard deviations from the mean (Fig. S3), but generally, the grain boundary systematic is suppressed.

The abrupt transitions in the power-stepped plasmon energy (Fig. 3F) and temperature (Fig. 3G) maps demonstrate thermalization within a 26-ms pixel time. Although the field of view was nearly isothermal at any given instant, the effective instantaneous temperature changes appear spatial because of the 22.5-min frame time. The mean temperature from each isothermal region is plotted in Fig. 3G as a function of the heater power. As expected for a small device in vacuum that is too cool to radiate appreciably, the temperature is linear in the applied power ($\theta$). When working either with devices or with lamellae deployed as local thermometers, a plot such as Fig. 3G is straightforward and fast to acquire and provides a translation between power and temperature that can be ported to situations in which direct measurements of the latter are not feasible.

With careful calibration we expect sub-1 K accuracies are possible because the physics underlying PEET is well understood on longer length scales (figs. S4 to S8) (21–23, 25). Heating by the electron beam is negligible. The temperature increment is roughly $\Delta T = \frac{I_d \sigma c}{m \Delta E}$ (28), where $I_d = 0.5$ nA is the beam current and $\sigma = 240$ W/K · m is aluminum’s thermal conductivity. Plasmons, the dominant source of energy loss, are created by the beam in a mean free path $l_m \sim 100$ nm, which gives $\Delta E / dx \sim 15$ eV/100 nm. The resultant $\Delta T$, less than 1 mK, is far below our current sensitivity. Using a furnace-style heating sample holder, we heated a sample from room temperature to 720 K, compared the PEET value with the holder’s thermocouple reading, and found that they agree to within 10% (fig. S4).

For the data presented here, the rastering electron beam (probe) size was 1 to 2 nm, and the pixel spacing was as small as 2 nm (26). Is it meaningful to consider the existence of distinct temperatures at such small length scales in a solid, and can PEET measure them? Measurements of the plasmon energy do not sample distinct volumes for separations smaller than the plasmon delocalization length $L_d$, which sets a resolution limit akin to the Rayleigh criterion (29). At 15.2 eV, the plasmon delocalization length $L_d \sim 100$ nm, which gives $\Delta T \approx 26$ K. The histograms in Fig. 2E show that the mean temperature difference $\sim 30$ K between each horizontal leg and its neighbor is resolved. Furthermore, the topmost and bottommost profiles have standard deviations that are comparable with the expected 8 K statistical noise, whereas the other histograms are generally broadened, reflecting the substantial temperature gradients in the horizontal legs and the absence of such gradients in the contacts.

Fig. 3. Rapid linear temperature changes. (A) Remote heater power versus time. (B) Plasmon energy scale for (E) and (F), and a combination temperature scale and histogram of the pixels of (G). (C and D) ADF STEM images corresponding to zero and variable power. In these 45- by 269-pixel images the beam was rastering from left to right, with a row time of 1.2 s, and then top to bottom. (E and F) Corresponding, simultaneously acquired plasmon energy maps. (G) Temperature map constructed from the normalized subtraction of (E) from (F). (H) Temperature extracted from (G) versus heater power, along with a linear fit (purple) and the corresponding fit parameters.
is 3 nm (29), which is consistent with the grain boundary widths (which correspond to atomic-scale features) seen in our plasmon energy maps (fig. S1). However, the sample does not support a temperature gradient for separations smaller than the electron mean free path \( \ell_p \), because electrons are ballistic over distances less than \( \ell_p \). Thus, \( \ell_p \) describes the smallest thermal feature size that can exist in continuous aluminum. Similarly, because phonons generate thermal expansion, temperature cannot produce different densities at separations smaller than a phonon mean free path \( \ell_\phi \). We estimate \( \ell_\phi \approx 4 \) to 15 nm and \( \ell_p \approx 2 \) to 5 nm in our temperature range (table S1). For \( \ell_\phi \) smaller than \( \ell_p \) or \( \ell_c \), PEET achieves the maximum possible spatial resolution; temperature differences do not exist on length scales smaller than the larger mean free path.

PEET is applicable to many other technologically important metals and semiconductors. Tungsten, silver, silicon, gallium arsenide, and gallium nitride all have sufficiently sharp plasmon resonances (29). [The width of the plasmon resonance limits PEET’s precision, so decreasing the zero loss peak width (30) gives only a small sensitivity improvement.] Because the product of the thermal expansion coefficient \( \alpha \) with the melting temperature is \( \alpha T_m \sim 0.02 \) for many materials (31), one will generally trade high sensitivity for a large accessible temperature range, or vice versa, depending on the application. Ideally, the system to be measured serves as its own thermometer, without requiring the introduction of thermometric materials that might compromise the thermal behavior or device function.

**REFERENCES AND NOTES**

24. Neglecting \( \alpha_s \) gives the simpler approximation \( \Delta T \sim 27/\ell_c^2 \), but accounting for the temperature dependence of \( \ell_c \) is necessary because the resulting correction of \( \Delta T\ell_c^2 \) is larger than our sensitivity.

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**EXOPLANET DYNAMICS**

**Asynchronous rotation of Earth-mass planets in the habitable zone of lower-mass stars**

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Planets in the habitable zone of lower-mass stars are often assumed to be in a state of tidally synchronized rotation, which would considerably affect their putative habitability. Although thermal tides cause Venus to rotate retrogradely, simple scaling arguments tend to attribute this peculiarity to the massive Venusian atmosphere. Using a global climate model, we show that even a relatively thin atmosphere can drive terrestrial planets’ rotation away from synchronicity. We derive a more realistic atmospheric tide model that predicts four asynchrony equilibrium spin states, two being stable, when the amplitude of the thermal tide exceeds a threshold that is met for habitable Earth-like planets with a 1-bar atmosphere around stars more massive than ~0.5 to 0.7 solar mass. Thus, many recently discovered terrestrial planets could exhibit asynchronous spin-orbit rotation, even with a thin atmosphere.

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A s we experience in our everyday life, atmospheric temperatures oscillate following the diurnal insolation cycle. This in turn creates periodic large-scale mass redistribution inside the atmosphere—the so-called thermal atmospheric tides. But as we all also have experienced, the hottest moment of the day is actually not when the Sun is directly overhead, but a few hours later. This is due to the thermal inertia of the ground and atmosphere that creates a delay between the solar heating and thermal response (driving mass redistribution), causing the whole atmospheric response to lag behind the Sun (1). Because of this asymmetry in the atmospheric mass redistribution with respect to the subsolar point, the gravitational pull exerted by the Sun on the atmosphere has a nonzero net torque that tends to accelerate or decelerate its rotation, depending on the direction of the solar motion (2,3). Because the atmosphere and the surface are usually well coupled by friction in the atmospheric boundary layer, the angular momentum transferred from the orbit to the atmosphere is then transferred to the bulk of the planet, modifying its spin (4). On Earth, this effect is negligible because we are too far away from the Sun, but the atmospheric torque due to thermal tides can be very powerful, as seen on Venus. Indeed, although tidal friction inside the planet is continuously trying to spin it down to a state of synchronous rotation, thermal tides are strong enough to drive the planet out of synchronicity and to force the slow retrograde rotation that we see today (2–6). Very simple scaling arguments predict that the amplitude of the thermal tide is proportional to the ratio of the atmospheric mean surface pressure over its scale height (7). Everything else being equal, one would thus expect the thermal tide to be ~50 times weaker if Venus had a less massive, cooler Earth-like atmosphere. Whether this scaling really holds and how massive the atmosphere...
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